## • Concept of tangent at any point of the circle

**Theorem:** The tangent at any point on a circle is perpendicular to the radius through the point of contact.

## **Example:**

A tangent AB at a point A of a circle of radius 6 cm meets a line through the centre O at the point B, such that OB = 10 cm. Find the length of AB.

# Solution:



It is known that the tangent at any point on a circle is perpendicular to the radius through the point of contact.

 $OA \perp AB$ 

By applying Pythagoras theorem in right triangle OAB, we obtain  $OA^2 + AB^2 = OB^2$   $\Rightarrow 6^2 + AB^2 = 10^2$   $\Rightarrow AB^2 = (100 - 36) \text{ cm}^2$   $\Rightarrow AB^2 = 64 \text{ cm}^2$  $\Rightarrow AB=64 \text{ cm}2=8 \text{ cm}$ 

No tangent can be drawn to a circle passing through a point lying inside the circle.

One and only one tangent can be drawn to a circle passing through a point lying on the circle.

Exactly two tangents can be drawn to a circle through a point lying outside the circle.

• Tangent drawn from an external point to a circle

**Length of the tangent:** The length of the segment of the tangent from an external point P to the point of contact with the circle is called the length of the tangent from the point P to the circle.





**Theorem:** The lengths of tangents drawn from an external point to a circle are equal.

# **Example:**

In the given figure, a circle is inscribed in  $\triangle$ ABC touching the points, P, Q, and R.



If AB = 7 cm, BC = 9 cm, CA = 8 cm, then find the measures of AR, AQ, BR, BP, CP, and CQ.

# Solution:

It is known that the lengths of tangents drawn from an external point to a circle are equal.

AR = AQ = a (say) BR = BP = b (say) CP = CQ = c (say)

AB + BC + CA = (7 + 9 + 8) cm = 24 cm

$$\Rightarrow (a+b) + (b+c) + (c+a) = 24 \text{ cm}$$
  
$$\Rightarrow 2(a+b+c) = 24 \text{ cm}$$
  
$$\Rightarrow a+b+c = 12 \text{ cm}$$

AB = 7 cm  $\Rightarrow a + b = 7 \text{ cm}$   $\therefore c + 7 \text{ cm} = 12 \text{ cm}$  $\Rightarrow c = (12 - 7) \text{ cm} = 5 \text{ cm}$ 

BC = 9 cm  $\Rightarrow b + c = 9$  cm  $\Rightarrow b = 9 - c = (9 - 5)$  cm = 4 cm

a + b + c = 12 cm  $\therefore 9 \text{ cm} + a = 12 \text{ cm}$  $\Rightarrow a = (12 - 9) \text{ cm} = 3 \text{ cm}$ 

Hence, AR = AQ = 3 cm, BR = BP = 4 cm,

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CP = CQ = 5 cm.

Results: If two tangents are drawn to a circle from an external point, then

1.

- 1.
- 2. 1. they subtend equal angles at the centre.
- 3. 2. they are equally inclined to the segment, joining the centre to that point.

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